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HAMILTONIAN SYSTEMS AND CELESTIAL MECHANICS

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PREFACE

The papers in this volume form a self-contained collection of lectures on Hamiltonian Systems and Celestial Mechanics. They are an outgrowth of the lectures that took place during the “International Symposium on Hamiltonian Systems and Celestial Mechanics”, which was held at CIMAT (Centro de Investigación en Matemáticas, Guanajuato, México) from September 30 to October 4, 1991. The emphasis of all the talks was on Hamiltonian Dynamics and Celestial Mechanics and their relationship to several aspects of topology, mechanics and dynamical systems in general. The Scientific organizers of the Conference were E.A. Lacomba and J. Llibre, the administrative organizer was K.B. Wolf on the part of CIFMA (Centro Internacional de Física y Matemáticas Aplicadas, Cuernavaca, México).

The symposium gathered together 41 researchers (13 from México and 28 from abroad), in addition to 17 graduate students, 38 lectures were given (4 of them by graduate students) during 32 session hours. All speakers were invited to submit a contribution to these proceedings. All papers that were received went through the refereeing process typical of a mathematical research journal and those that were accepted form the present volume.

The organization and realization of the meeting was possible due to a lot of work on the part of a number of people. First, thanks are due to Bernardo Wolf and Petra Seligman from the CIFMA who took care with great enthusiasm of the logistic administration of the meeting and many other things. Fausto Ongay and the staff at CIMAT have been particularly helpful in providing all their facilities for the realization of the meeting. We are also indebted to Joaquín Delgado and Ernesto Pérez Chavela for their collaboration and support in the preparation and realization of the symposium. We must thank the economical support provided by the following institutions. From México the CONACYT, the Universidad Autónoma Metropolitana, and the Universidad Nacional Autónoma de México; from Spain CIRIT and DGICYT; from the International Center of Theoretical Physics in Trieste. And last but not least, the participants at the Conference must be thanked for offering everyone a week-long intense and highly interesting mathematical experience.

Ernesto A. Lacomba and Jaume Llibre

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